## List of Theorems for Mth 435 Final

Parts of the proofs of the following theorems could appear on the final exam.

- 1. Theorem 0.7 Equivalence of well-ordering principle, mathematical induction and strong induction.
- 2. Theorem 1.18 Between any two distinct real numbers, there is a rational and an irrational number.
- 3. Theorem 1.25 A countable union of countable sets is countable.
- 4. Theorem 2.10 A bounded monotone sequence is convergent.
- 5. Theorem 2.13 A sequence of real numbers is convergent if and only if it is Cauchy.
- 6. Theorem 2.18 Every sequence of real numbers has a monotone subsequence.
- Theorem 2.19
  Bolzano-Weierstraß- A bounded sequence of real numbers has a convergent subsequence (you should know both proofs, that using monotone subsequences and the one in the homework using subdvision).
- 8. Theorem 3.16 The Intermediate Value Theorem
- 9. Theorem 3.17 The Extreme Value Theorem
- 10. Theorem 3.28 f continuous on  $[a, b] \Longrightarrow f$  uniformly continuous on [a, b].
- 11. Theorem 4.11 Rolle's Theorem
- 12. Theorem 4.12 The Mean Value Theorem